**Problem 1**

Question 1

All we need to prove is that there exists a group of 3 points shattered by , but every group of 4 points cannot be shattered by .



Now let's look at a set of 4 points, . Assume without loss of generality that they are ordered in the following order in . If is closer to than is to , then by looking at labeling (1) no circle could cover without including or . Similarly, we can prove that if is farther from than is to , no circle could cover without including or . Therefore, for any group of points of size 4, doesn't shatter it, and thus .

a

b

c

d

Note: diagrams are disgusting sorry 😊

Question 2

Question 3

The problem is now PAC learnable, therefore, according to the fundamental theorem of statistical learning:

**Problem 4**

Section a

We want to find local minimum, which can be done by finding points where function gradient of is 0.